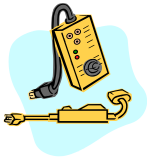


SINGLE-PHASE RECTIFIERS WITH CAPACITIVE FILTER



I. OBJECTIVES

- To establish the dependence between the type of the rectifier (half-wave and full-wave) and the shape of the rectified voltage.
- To determine how the load resistor and the values of the filtering capacitor influence the rectified voltage.
- To deduce the maximum reverse voltage on the rectifying diodes.



II. COMPONENTS AND INSTRUMENTATION

For the experiment you will use an experimental board, a transformer, four rectifying diodes, two electrolytic capacitors, a resistor and a potentiometer. In order to visualise the voltages you will use a dual channel oscilloscope, a voltmeter and an ammeter for the measurement of the average values of the voltage and current.



III. THEORETICAL ASPECTS

1. Half-wave rectifiers

1.1. Half-wave rectifiers with resistive load

The voltage v_I is obtained from the secondary of a transformer, with a ratio of 23:1. The primary voltage comes from the outlet and is a sinewave, with 230V effective value and 50 Hz frequency.

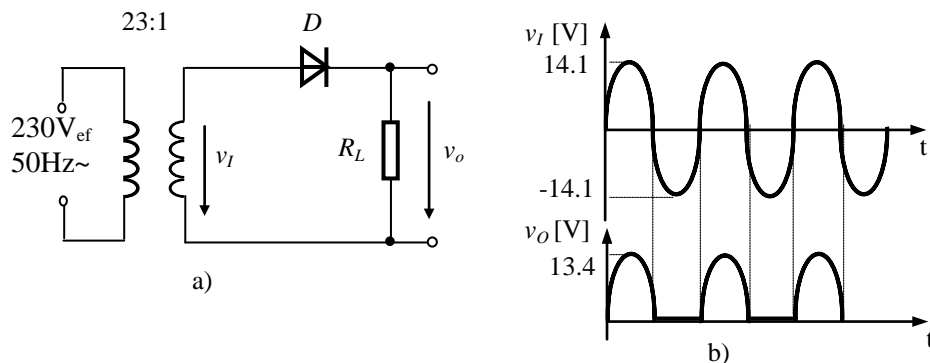


Fig. 1. Half-wave rectifier a) Circuit; b) Waveforms;

The amplitude of v_I is computed as follows:

$$n = 23 = \frac{\hat{V}_{primary}}{\hat{V}_{secondary}}$$

$$\hat{V}_{\text{secondary}} = \hat{V}_I = \frac{\hat{V}_{\text{primary}}}{23} = \frac{230\sqrt{2}}{23} = 14.1V$$

1.2. Half-wave rectifiers with capacitive filter

Rectifiers with D and R (for example the half-wave rectifier in Fig. 1) generate an output voltage of a single sign, but it has a considerable variation, equal to the amplitude of the input signal. To obtain a continuous voltage, we must smoothen these variations by adding a filtering capacitor (see Fig. 2).

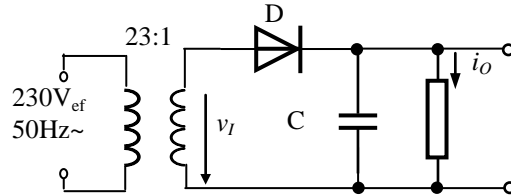


Fig. 2. Half-wave rectifier with capacitive filter

The circuit can be seen also as a positive peak detector loaded with R . In actual practical situations, such as the design of power supplies a load resistance will be inherently present. If the input voltage is an alternative sinusoidal one, between two consecutive peaks of v_I , the capacitor will discharge through R and v_O will go down, unlike the situation without R when v_O was constant (see Fig.2.4.2). The waveforms in steady-state regime for the circuit in Fig. 2 are plotted in Fig. 3. The time constant of the circuit, RC , should be much greater than the period T of the signal, $RC \gg T$. Note that the output is no longer a constant dc voltage but it may be considered as being composed on a dc voltage on which an ac component, called *ripple*, is superimposed.

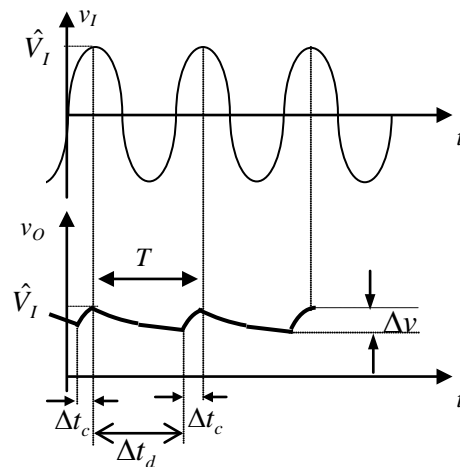


Fig. 3. Waveforms for half-wave rectifier with capacitive filter.

We specify the followings:

- The diode D conducts for short time intervals Δt_c , close to the positive peaks of v_I . We neglect the voltage drop across the conducting diode. The capacitor charges with an electric charge equal to the one lost on the longest duration of the discharge, Δt_d .

$$v_c(t) = (1 - e^{-\frac{t}{RC}})V_\infty + V(0) \cdot e^{-\frac{t}{RC}}$$

- When D *(off)*, C discharges through R and in this way v_O drops exponential with the time constant RC . At the end of the discharge interval Δt_d , which is almost equal with T , $v_O = \hat{V}_I - \Delta v$, where Δv is the peak to peak value of the ripple of the output voltage. If $RC \gg T$, Δv is small. A special attention will be paid to this ripple Δv .

We remind the expression of the voltage across the capacitor.

$$v_c(t) = (1 - e^{-\frac{t}{RC}})V_\infty + V(0)e^{-\frac{t}{RC}}$$

Let us assume the initial time moment, $t=0$ as being the moment when the discharge of the capacitor begins (v_I at the maximum value), therefore $V(0) = \hat{V}_I$. V_∞ is the value at which the voltage on the capacitor could finally reach, if the input signal will disappear, $V_\infty = 0V$. The time interval in which we are interested is the one of the capacitor's discharge $t = \Delta t_d$, when the value of the voltage is:

$$v(\Delta t_d) = \hat{V}_I - \Delta v$$

We obtain:

$$\hat{V}_I - \Delta v = \hat{V}_I e^{-\frac{\Delta t_d}{RC}} \approx \hat{V}_I e^{-\frac{T}{RC}}$$

Because $RC \gg T$ we can use the approximation:

$$e^{-\frac{T}{RC}} \approx 1 - \frac{T}{RC}$$

$$\hat{V}_I - \Delta v = \hat{V}_I - \frac{T}{RC} \hat{V}_I$$

$$\Delta v = \frac{T}{RC} \hat{V}_I$$

The higher the time constant RC (usually by choosing a large value for C), the smaller is the ripple, so v_o is closer to a smooth continuous voltage.

Remark: An alternative interpretation of the previous approximation is that, on the intervals Δt_d we consider that the discharge of the capacitor happens at a constant current $I_o = \frac{\hat{V}_I}{R}$. This interpretation holds as long as $\Delta v \ll \hat{V}_I$

$$\Delta v = \frac{T}{C} I_o = \frac{T}{RC} \hat{V}_I$$

If we want to use the frequency f of the voltage:

$$\Delta v = \frac{1}{fC} I_o = \frac{1}{fRC} \hat{V}_I$$

2. Full-wave rectifiers

2.1. Full-wave rectifiers with resistive load

The schematic of the full-wave rectifier with resistive load is depicted in Fig. 4. The input and output voltages are plotted in Fig. 5.

On the positive half cycle of v_I , D_1 and D_3 are in conduction (while D_2 and D_4 are cutoff), and on the negative half wave D_4 and D_2 are in conduction (D_1 and D_3 being cutoff).

If we consider $0.7V$ across the conducting diodes, the amplitude of the output voltage is with $2 \cdot 0.7V = 1.4V$ less than the amplitude of the input voltage.

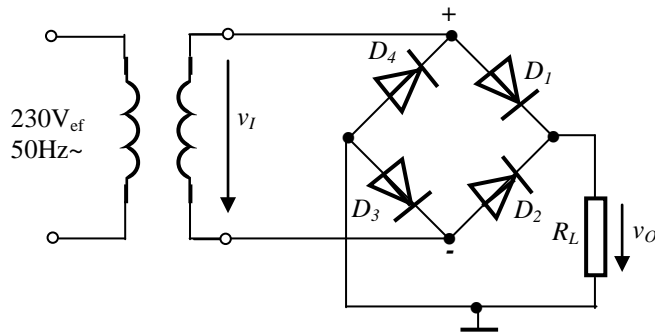


Fig. 4. Full-wave diode bridge rectifier

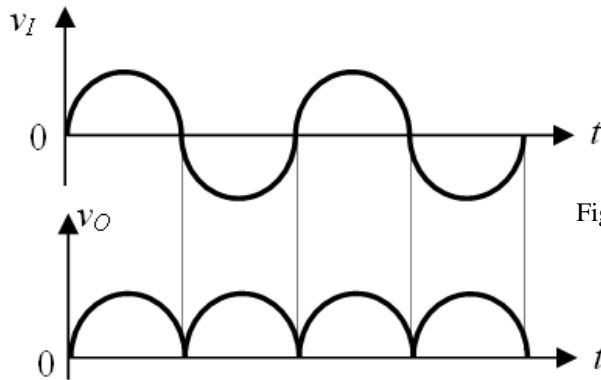


Fig. 5. Full-wave diode bridge rectifier - waveforms

2.1. Full-wave rectifiers with capacitive filters

In the case of a full-wave rectifier with capacitive filter (Fig. 6.), the reasoning is the same, just that the discharge time of the capacitor is shorter, approximately half of a period (Fig. 7).

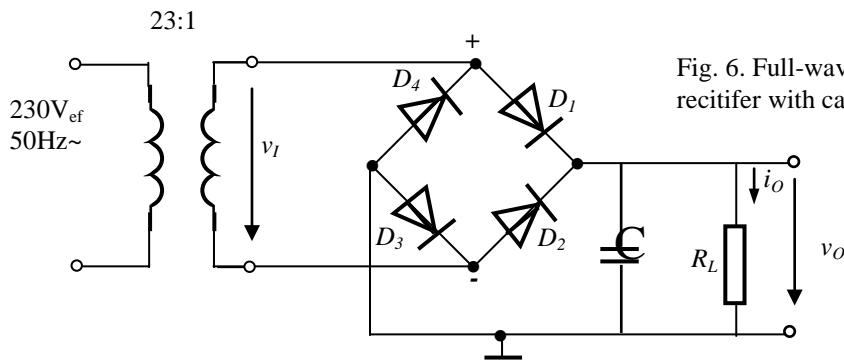


Fig. 6. Full-wave diode bridge rectifier with capacitive filter

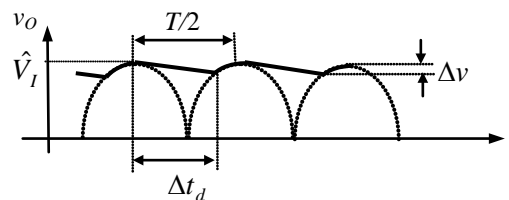


Fig. 7. Full-wave rectifier with capacitive filter - waveforms

In this case we have the relationship:

$$\Delta v = \frac{\hat{V}_I}{2fRC} \quad \text{or} \quad \Delta v = \frac{1}{2fC} I_O$$

Using the same capacitance, in the case of full-wave rectifier, the output ripple will be two times smaller.



IV. PREPARATION

1.P. SINGLE-PHASE HALF-WAVE RECTIFIER

1.1.P. SINGLE-PHASE HALF-WAVE RECTIFIER WITH RESISTIVE LOAD

- How do the waveforms for v_s , v_o and i_o look like for the circuit shown in Fig. 8 .if the transformer's ratio is $n = 23$?
- How can you compute the average value (DC component) V_o of the output voltage?
- What is the value of the output voltage ripple ΔV_o (the difference between the maximum and minimum value)?
- What is the value of the maximum reverse voltage on the rectifying diode?

1.2.P. SINGLE-PHASE HALF-WAVE RECTIFIER WITH CAPACITIVE FILTER

- How do the waveforms for v_s and v_o look like, for the circuit shown in Fig. 9?
- Compare the output voltage ripple for this circuit with the one obtained at 1.1.P.

2.P. SINGLE-PHASE FULL-WAVE RECTIFIER

2.1.P. SINGLE-PHASE FULL-WAVE RECTIFIER WITH RESISTIVE LOAD

All the points below refer to the circuit shown in Fig. 10.

- What are the states (on/off) of the four diodes, for the positive wave of the v_s voltage?
- How do the waveforms of v_s and v_o look like?
- Compare the output voltage ripple for this circuit with the one obtained at 1.1.P.

2.2.P. SINGLE-PHASE FULL-WAVE RECTIFIER WITH CAPACITIVE FILTER

- How does the output voltage look likes for the circuit in Fig. 11?
- Compare the output voltage ripple for this circuit with the one obtained at 2.1.P.

V. EXPLORATIONS AND RESULTS



*Notes: The sinusoidal voltage, which should be rectified in this experiment, is obtained from the transformer, T_r , as you can see in Fig. 8. The voltage source used as rectifier is a floating one. Because the primary of the transformer is connected to the voltage from the main network, be careful **not to touch** this part of the transformer when it is plugged in, because you can be **electrocuted!!!***

1. SINGLE-PHASE HALF-WAVE RECTIFIER

1.1 SINGLE-PHASE HALF-WAVE RECTIFIER WITH RESISTIVE LOAD



Exploration

Build the circuit shown in Fig. 8.

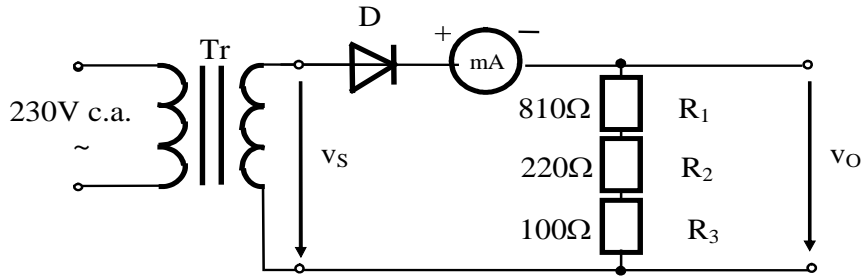


Fig. 8. Single-phase half-wave rectifier

For three combinations of the load resistance, ($R_1 + R_2 + R_3$, $R_2 + R_3$, R_3), do the following:

- With the dual channel oscilloscope, calibrated, set on Y-t mode, visualise v_s and v_o .
- With a DC voltmeter, measure the value of the dc component of V_o .
- Measure (read) the output voltage ripple, ΔV_o , from the oscilloscope.
- With the dc milliammeter set on **200mA**, measure the dc component of I_o (load current).



Results

- $v_s(t)$ and $v_o(t)$ for the load resistance $R_1 + R_2 + R_3$
- Fill in Table 1 – the rows with $C = 0\mu\text{F}$.

Table 1

	R_L [Ω]	$R_1 + R_2 + R_3$	$R_2 + R_3$	R_3
	C [μF]			
	0			
I_o [mA]	100			
	1000			
	0			
V_o [V]	100			
	1000			
	0			
ΔV_o [V]	100			
	1000			

1.2 SINGLE-PHASE HALF-WAVE RECTIFIER WITH CAPACITIVE FILTER



Exploration

Build the circuit shown in Fig. 9.

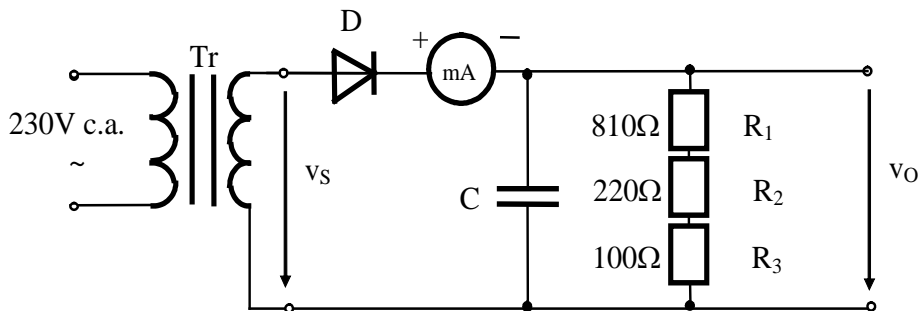


Fig. 9. Single-phase half-wave rectifier with capacitive filter

a) C=100 μ F

Follow the steps from experiment 1.1.

b) C=1000 μ F

Follow the steps from experiment 1.1.



Results

a) C=100 μ F

- $v_S(t)$ and $v_O(t)$ for the load resistance $R_1 + R_2 + R_3$
- Fill in Table 1 – the rows with $C = 100\mu\text{F}$.

b) C=1000 μ F.

- Fill in Table 1 – the rows with $C = 1000\mu\text{F}$.

2. SINGLE-PHASE FULL-WAVE RECTIFIER

2.1 SINGLE-PHASE FULL-WAVE RECTIFIER WITH RESISTIVE LOAD



Exploration

Build the circuit shown in Fig. 10.

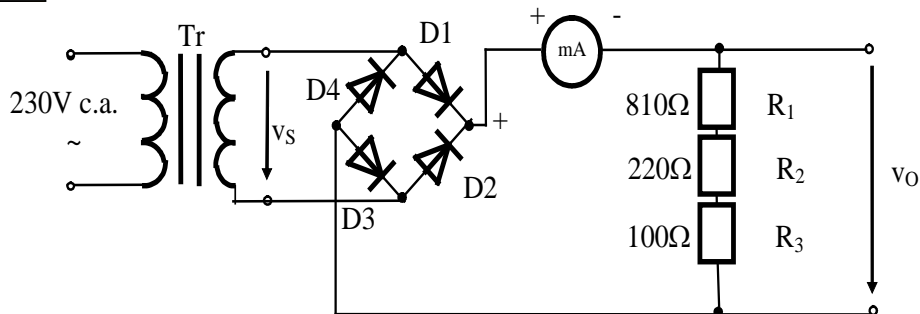


Fig. 10. Single-phase full- wave rectifier

For three combinations of the load resistance, ($R_1 + R_2 + R_3$, $R_2 + R_3$, R_3), do the following:

- With the dual channel oscilloscope, calibrated, set on Y-t mode, visualise v_S and v_O .
- With a DC voltmeter, measure the value of the dc component of V_O .
- Measure (read) the output voltage ripple, ΔV_O , from the oscilloscope.
- With the dc milliammeter set on **200mA**, measure the dc component of I_O (load current).



Results

- $v_S(t)$ and $v_O(t)$ for the load resistance $R_1 + R_2 + R_3$
- Fill in Table 2 (identical to Table 1) – the rows with $C = 0\mu\text{F}$.

2.2 SINGLE-PHASE FULL-WAVE RECTIFIER WITH CAPACITIVE FILTER



Exploration

Build the circuit shown in Fig. 11.

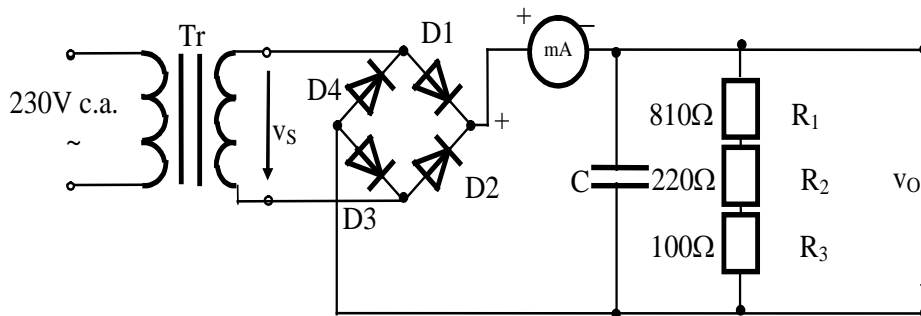


Fig. 11. Single-phase full-wave rectifier with capacitive filter

a) $C=100\mu\text{F}$

Follow the steps from experiment 2.1.

b) $C=1000\mu\text{F}$

Follow the steps from experiment 2.1.



Results

a) $C=100\mu\text{F}$

- $v_S(t)$ and $v_O(t)$ for the load resistance $R_1 + R_2 + R_3$
- Fill in Table 2 – the rows with $C = 100\mu\text{F}$.

b) $C=1000\mu\text{F}$

- Fill in Table 2 – the rows with $C = 1000\mu\text{F}$.

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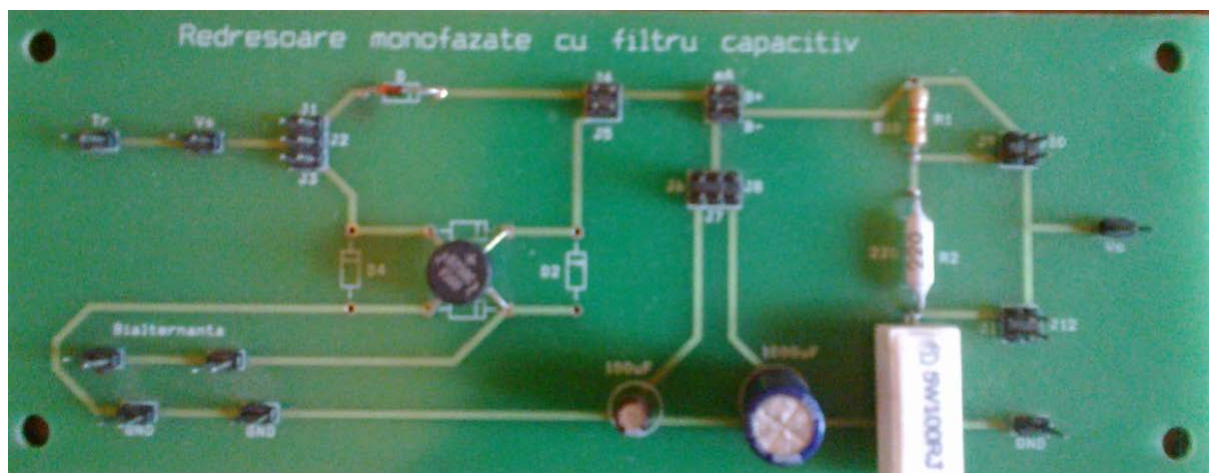


Fig. 12. Experimental assembly